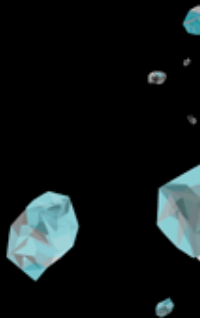
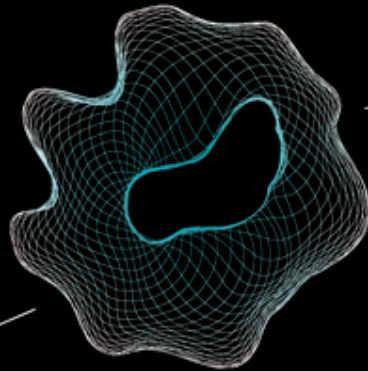


**Module 8: Programming Paradigms**  
***Logic Programming***  
**part 1: facts, rules & queries**

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# Schedule LP

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- Three lectures: May 14th, 16th, 22nd (block 4,5)
- Visit them: not all I say is on the slides.
- Idea:
  - 1 hour construction (lecture + instruction)
  - 3 hours practical exercises (signed off, in pairs)
  - You should already start with the project in block 5.
- LP project: May 21 - May 28 (block 5)
  - Work on the project (handed in, in pairs)
  - Last session on May 28, deadline on May 29th.
- **All material:**
  - Canvas, Block 4,5 (reader, labfiles)
  - Tooling (SWI-Prolog)



# Overview

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## 1. Facts, rules & queries by Example:

- Example: The Royal Family (exercise 1)

## 2. Structured objects with function symbols (terms)

## 3. Problem solving by Example:

- Example: Monkey and Banana (exercise 2)

## 4. Lists: recursion and backtracking

- Lists and Tree-sort (exercise 3)

# Prolog – logic programming

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A Prolog program consists of set of **clauses** (facts and rules).

You “run” Prolog by asking a **query**.

Prolog tries to find a **proof** of the query from the facts and rules.

It does so by systematic search, depth-first, using **backtracking**.

Here is your first Prolog program:

```
a:-b.      % a follows from b  
a:-c, d.   % a follows from c and d  
c.        % c is a true fact  
d:-c.     % d follows from c
```

When asked to prove the query **a**:

- First, Prolog tries to prove **b**, which fails.
- Then it is tried to prove **c** and **d**.
  - **c** is a fact, so this holds
  - for **d**, we must prove **c** (again), this will succeed.

# Predicates, terms, variables

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Predicates (like **a,b,c** on the previous slide) can have arguments:

Every argument is a term. For now, we a term can be:

1. An atom: lower case identifier, denotes a fixed object or number
2. A variable: upper case identifier, can be bound to any object

**Given Clauses (the program consists of these two facts):**

**age(john,33).**

**age(peter,21).**

**Queries:**

**Results:**

**?- age(john,33).**

**yes / true**

**?- age(john,21).**

**no / false**

**?- age(X,21).**

**X=peter**

**?- age(John,21).**

**John=peter**

**?- age(john,X).**

**X=33**

**?- age(X,Y).**

**X=john, Y=33;**

**X=peter, Y=21;**

Prolog returns either **no**, or **yes** with a list of **bindings** for the logical variables

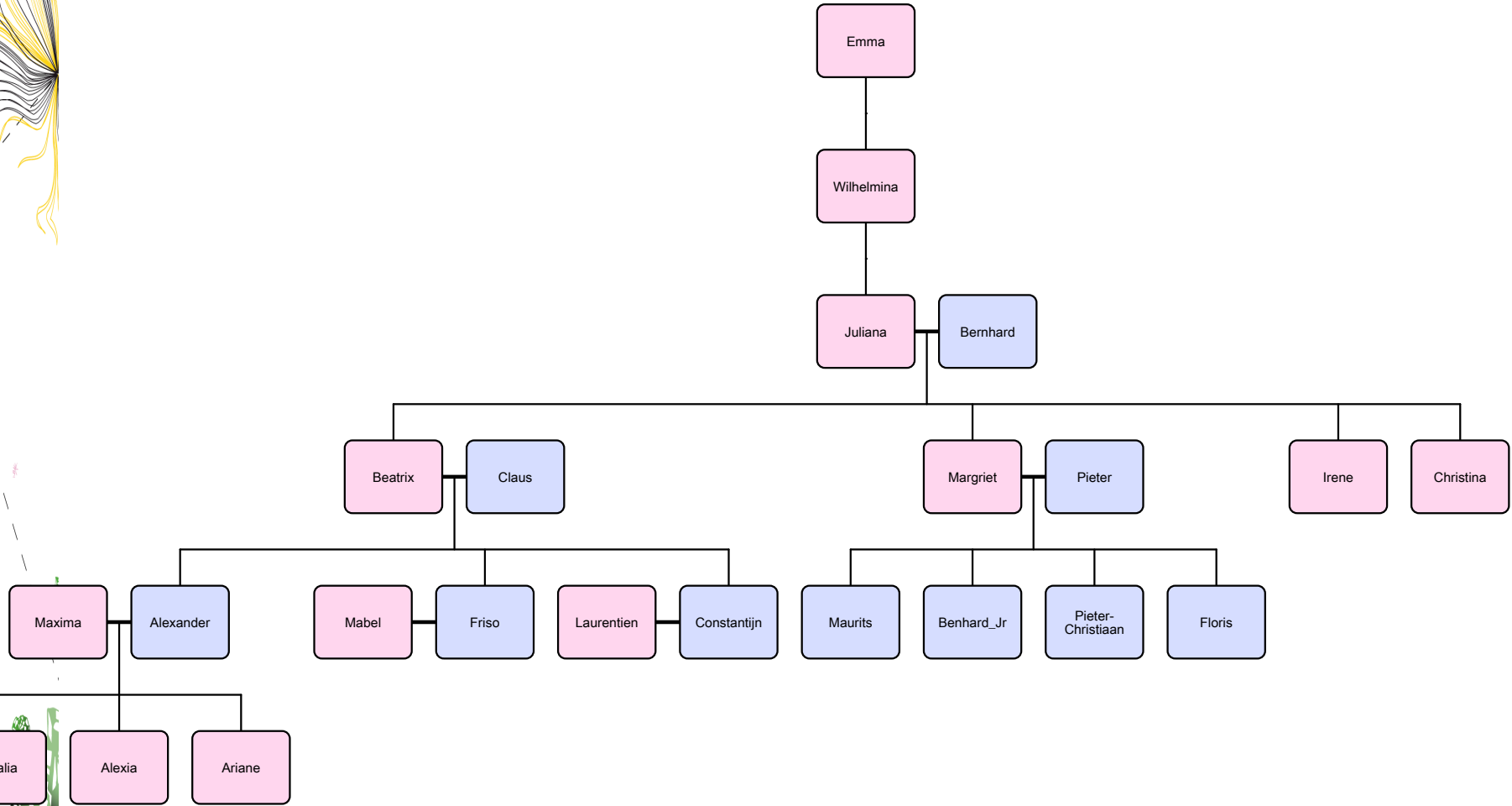
# Example: Royal family (fact database)

mother(emma,wilhelmina).  
mother(wilhelmina,juliana).  
mother(juliana,beatrix).  
mother(juliana,margriet).  
mother(juliana,irene).  
mother(juliana,christina).  
mother(maxima,amalia).  
mother(maxima,alexia).  
mother(maxima,ariane).  
...  
husband(bernhard,juliana).  
husband(claus,beatrix).  
husband(pieter,margriet).  
husband(alexander,maxima).

female(irene).  
female(amalia).  
...  
female(X) :- mother(X,\_).  
female(X) :- husband(\_,X).  
  
male(maurits).  
male(floris).  
...  
male(X) :- husband(X,\_).

Note, we have used  
don't care variables: \_

# Royal Family



# Interpretation of clauses

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**mother(maxima,amalia)** is interpreted (by us, not by Prolog)  
as: *maxima is the mother of amalia.*

**father(X,Y) :- husband(X,Z), mother(Z,Y).**

means: *for each X, Y and Z: X is the father of Y,  
if X is the husband of Z and Z is the mother of Y.*

**child(X,Y) :- father(Y,X).**

**child(X,Y) :- mother(Y,X).**

means: *for each X and Y: X is a child of Y, if  
Y is the father of X, or Y is the mother of X.*

Alternative (; means “or”)

**child(X,Y) :- father(Y,X) ; mother(Y,X).**

# Clauses: facts, rules, queries

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- A **clause** is of the form  **$h \text{ :- } b_1, \dots, b_n$** .
  - Here  $h, b_1, \dots, b_n$  are called *literals*.
  - Facts, rules and queries are all clauses:
- A **rule** is a clause with a non-empty head and body:
  - **$h$**  is the *head* of the rule
  - **$b_1, \dots, b_n$**  is the *body* of the rule
- A **fact** is a clause with an empty body:
  - **$h$** .
- A **query** is a clause with an empty head:
  - **$\text{:- } b_1, \dots, b_n$** . Sometimes also written as:  **$\text{?- } b_1, \dots, b_n$** .



## Exercise (1)

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1. Download SWI-prolog from <http://www.swi-prolog.org>.
2. Download the Prolog program "royal\_family\_facts" from Canvas. (in the zip: PP->Materials->block5)
3. Start Prolog with this program.
4. Evaluate each of the following queries, first by inspecting the program, then by using Prolog.
  - a: **?- mother(juliana,Beatrix).**
  - b: **?- female(X).**
  - c: **?- husband(X,Y).**
5. Write a predicate **grandfather/2**.
6. Write a predicate **sister/2**.

## Exercise (2)

### Solutions:

**grandfather(X,Y):- child(Y,Z),child(Z,X),male(X).**

**sister(X,Y) :- child(X,P), female(X), child(Y,P), not(X=Y).**

This exercise is continued later during exercise class,  
By writing and testing predicates like grandson, aunt, cousin...

Let's write a recursive program:

**ancestor(X,Y) :- child(Y,X).**

**ancestor(X,Y) :- child(Y,Z) , ancestor(X,Z).**

Try:

**?- ancestor(X,amalia).**

**?- ancestor(X,maurits) , ancestor(X,alexia).**

Will this predicate always “terminate”? Why? When?

# The paradigm of Logic Programming, so far

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- Allows a very free format:
  - We didn't have to provide any declaration, just facts and rules
  - The only "convention" is the distinction upper/lower case
- No pre-determined computation order, you can freely mix "forward" and "backward" computations
- That is: Prolog works with **relations**, not with **functions**
- **Beware**: Prolog uses a *closed world assumption*
  - **?- husband(X,emma). No.**
  - *In reality she did have a husband, but he wasn't in the database*



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## 4. Lists: recursion and backtracking

- Lists and Tree-sort (exercise 3)



# Structured data

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- Data can be structured, like in
  - date(23, may, 2016)**
  - triangle(point(4,5),point(5,9),point(13,3))**
- In general, terms consist of:
  - **atoms (lower-case identifiers, numbers)**
  - **variables (upper-case identifiers)**
  - **function application  $f(t_1, \dots, t_n)$ , where  $t_i$  are terms**
- Prolog allows infix notation, like  $1+3$ ,  $1=<5$ 
  - Here  $+$  and  $=<$  are the function symbols
- Special list notation:  $[]$ ,  $[\text{Head}|\text{Tail}]$ 
  - $[]$  is a constant, and  $[_ | _]$  is a binary function symbol

# Terms and unification

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- Variables can be used for “pattern matching”
- For instance:
  - **?- date(23,may,2016) = date(Day,Month,Year).**  
Yes. [Day=23, Month=may, Year=2016]
  - **?- point(3,4)=point(X,\_).**  
Yes. [X=3]
  - **?- f(X,f(Y)) = f(f(Z),Z).**  
Yes. [X=f(f(Y)), Z=f(Y)]
- In general, **term1 = term2** checks if these two terms can be made equal by substituting terms for the variables.
- Prolog always computes *the most general unifier*

# Lists and the typical list recursion

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Lists are just terms, using a special function-notation.

Lists in Prolog are inhomogeneous: elements can be any terms.

**Notation:** `[]` is the empty list

`[X]` is the list with single element **X**

`[X|Y]` is the list with head **X** and tail **Y**

`[X,Y|Z]` is the list with elements **X** and **Y** and tail **Z**

The predicate `member/2` tests if an element is in the list:

`member(X,[X|_]).`

`member(X,[_|L]) :- member(X,L).`

The predicate `append/3` concatenates two lists

`append([],Xs,Xs).`

`append([X|Xs],Ys,[X|Zs]) :- append(Xs,Ys,Zs).`

**Note:** this function can be used in many ways!!



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  - Lists and sorting (exercise 3)

# Monkey gets Banana

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- Prolog is good at problem solving
- We will go through a very simple planning problem:
- A monkey wants a banana hanging from the ceiling
- For this, he must walk to a box, push it, climb it
- We model “*the state of the world*” a structure:  
**state(Monkey, Position, Box, Has)**
  - **Monkey** is the location of the monkey (atdoor, atwindow, middle)
  - **Position** is the position of the monkey (onfloor, onbox)
  - **Box** is the location of the box (atdoor, atwindow, middle)
  - **Has** indicates if the Monkey has the banana (has, hasnot)



# The actions of the Monkey

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The monkey can perform several actions, between two states of the form **state(Monkey,Position,Box,Has):**

- **grab** - grab the banana
  - **climb** - climb on top of the box
  - **walk(Pos1,Pos2)** - walk to from position 1 to 2
  - **push(Pos1,Pos2)** - push the box from Pos 1 to 2
- 
- The actions are only possible under certain conditions, *which we must define by rules in the program*
  - Will the monkey be able to grab the banana? *which we must formulate as a query*

# Goal and Moves

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- The initial state can be described by the term:  
**state(atdoor,onfloor,atwindow,hasnot)**
- The goal states can be described by the term:  
**state(\_,\_\_,\_ ,has)**
- We describe the possible actions by a predicate move/3:  
**move(State1,Action,State2).**
- If the monkey is on the floor at the box, it can climb it:  
**move(state(Pos, onfloor, Pos, Has),  
climb,  
state(Pos, onbox, Pos, Has) ).**
- **Exercise:** describe the other actions: **grab, walk, push**

# A generic problem solver in Prolog

---

- We can now write a very simple and general solver:

```
solve(state(_,_,_,has)).
```

```
solve(State1):- move(State1,Move,State2), solve(State2).
```

- Now Prolog can automatically solve the problem:  
**?- solve(state(atdoor,onfloor,atwindow,hasnot)).**  
**Yes.**
- **Exercise 2 today:**
  - Finish the whole puzzle.
  - Let Prolog compute a concrete sequence of actions.



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# Exercise

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1. Write a predicate **quicksort**, which sorts a list using the well-known quicksort-algorithm.
2. Write a predicate **slowsort**, which sorts a list by searching through all permutations of the list for a sorted one.

We will use the built-in comparison operator:

**M =< N**

# Solution for slowsort

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**slowsort(X,Y) :- perm(X,Y), sorted(Y).**

**sorted([]).**

**sorted([X]).**

**sorted([X,Y|Z]) :- X=<Y, sorted([Y|Z]).**

**perm([],[]).**

**perm([X|Y],Z) :- perm(Y,A), insert(X,A,Z).**

**insert(X,A,[X|A]).**

**insert(X,[K|S],[K|R]) :- insert(X,S,R).**



# Solution for quicksort

---

```
quicksort([],[]).
```

```
quicksort([A|B],C) :-
```

```
    split(A,B,D,E),
```

```
    quicksort(D,F),
```

```
    quicksort(E,G),
```

```
    append(F,[A|G],C).
```

```
% split(A,B,D,E): Split list B in D and E by comparing with A
```

```
split(X,[],[],[]).
```

```
split(X,[A|B],[A|C],D) :- A=<X, split(X,B,C,D).
```

```
split(X,[A|B],C,[A|D]) :- A>X, split(X,B,C,D).
```



# General approach to Prolog programming

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## 1. Declarative step: Model the problem

- Decide which structures to use (function symbols)
- Define the important relations (predicates)

## 2. Algorithmic step: Write a general solver

- Independent from the problem

## 3. Procedural thinking: Make it work

- Take into account termination (order of rules)
- Take into account efficiency, search strategy, pruning

Largest pitfall: Start too early thinking procedurally