

Searching

Linear : $c*n$

Binary: $c*\log_2 n$

Sorting:

Bubble: n^2

Linear: bestcase: $c2*n$

Worst: $c1*n^2$

Merge: $n*\log_2 n$

Merge sort (pseudo-code)

```
if data has 0 or 1 element(s) then
  return a copy of data
else
  Sort the first half of data and assign the result to fst;
  Sort the second half of data and assign the result to snd;
  Assign an empty list to res;
  Assign 0 to fi and si;
  while fi and si are valid indexes in fst and snd, respectively do
    if fst[fi] < snd[si] then
      Append fst[fi] to res;
      Increase fi by one;
    else
      Append snd[si] to res;
      Increase si by one;
    end
  end
  if fi is a valid index in fst then
    Glue the rest of fst (from fi onwards) to the end of res ;
  else if si is a valid index in snd then
    Glue the rest of snd (from si onwards) to the end of res ;
  end
  return res
end
```

zipping

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Pearl 001: Algorithmics - Sorting

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```
1 def linear(data, value):
2   """Return the index of 'value' in 'data', or -1 if it does not occur"""
3   # Go through the data list from index 0 upwards
4   i = 0
5   # continue until value found or index outside valid range
6   while i < len(data) and data[i] != value:
7     # increase the index to go to the next data value
8     i = i + 1
9   # test if we have found the value
10  if i == len(data):
11    # no, we went outside valid range; return -1
12    return -1
13  else:
14    # yes, we found the value; return the index
15    return i
```

Algorithm 2: Binary search in an ordered list

input : Ordered, non-empty *data* and target value *val*

output: The index of *val* in *data*, or -1 if *val* does not occur in *data*

```
1 Assign to low and high the first and last index in data;
2 while interval between low and high non-empty and  $data[low] \neq val$  do
3   Choose mid in the middle between low and high ;
4   if  $data[mid] = val$  then
5     Assign to low the value of mid ; /* Found! */
6   else if  $val < data[mid]$  then
7     Assign to high the value of  $mid - 1$ ; /* val lies before index mid */
8   else
9     Assign to low the value of  $mid + 1$ ; /* val lies after index mid */
10  end
11 end
12 return if  $data[low] = val$  then low, otherwise  $-1$ 
```

Algorithm 3: Ordering a list using bubble sort

```

input : List data
output: Sorted copy of list data
1 Assign a copy of data to res ; /* res is the result list */
2 Assign the last index in res to ui ; /* ui is the index of the last unsorted value */
3 while ui > 0 do /* If ui equals 0, everything is sorted */
4   Assign 0 to si ; /* si is the index of the last swapped value */
5   Assign 0 to i ; /* i is the index that is currently processed */
6   while i < ui do /* If ui is reached then the rest is ordered */
7     if res[i] > res[i+1] then /* res[i] en res[i+1] are inverted */
8       Swap res[i] and res[i+1] ;
9       Assign i to si ; /* We just swapped at index i */
10    end
11    Increment i by one;
12  end
13  Assign si to ui ; /* The list is ordered from si+1 */
14 end
15 return res
  
```

$$3//2 = 1$$

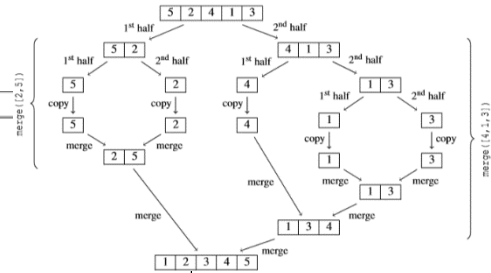
$$3/2 = 1.5$$

$$3\%2 = 1$$

Algorithm 4: Ordering a list using merge sort

```

input : List data
output: Sorted copy of list data
1 if data has 0 or 1 element(s) then
2   return a copy of data
3 else
4   Sort the first half of data and assign the result to fst ;
5   Sort the second half of data and assign the result to snd ;
6   Assign an empty list to res ; /* res is the result list */
7   Assign 0 to fi and si ; /* fi and si are increasing indexes in fst and snd */
8   while fi and si are valid indexes in fst and snd, respectively do
9     if fst[fi] < snd[si] then /* fst[fi] is smaller than snd[si] */
10      Append fst[fi] to res ;
11      Increase fi by one;
12    else /* snd[si] is smaller than (or equal to) fst[fi] */
13      Append snd[si] to res ;
14      Increase si by one;
15    end
16  end
17  if fi is a valid index in fst then
18    Glue the rest of fst (from fi onwards) to the end of res ; /* All snd-elements have been treated */
19  else if si is a valid index in snd then
20    Glue the rest of snd (from si onwards) to the end of res ; /* All fst-elements have been treated */
21  end
22  return res
23 end
  
```



Binary faster when:

For 1000 distinct words

$$10 * N + 10000 < 1000 * N$$

$$990N > 10000$$

$N \geq 10$ When searching 10 times or more

Algorithm 5: Removing duplicates

```

input : Sorted list data
output: Copy of data in which each value occurs exactly once
1 Assign an empty list to res ;
2 if data is not empty then /* res is the result list */
3   Assign data[0] to fresh ; /* If data is empty, data[0] does not exist */
4   Assign 1 to i ; /* fresh is a fresh value not yet occurring in res */
5   while i is a valid index in data do /* Continue until the end of data */
6     if data[i] does not equal fresh then /* We arrived at the next distinct value */
7       Append fresh to res ; /* The previous fresh value is added to res */
8       Assign to fresh the value of data[i] ; /* This is the next fresh value */
9     end
10    Increment i by one;
11  end
12  Append fresh to res ; /* The last fresh value is appended to res */
13 end
14 return res
  
```