

1. Sketch the domain of the functions given below. In the sketch, axes must be labeled and supplied with numbers, and the domain is shaded. See figure 14.4, *Thomas' Calculus*, p. 767.

(a) $f(x, y) = \ln(x^2 + y^2 - 4)$.

(b) $f(x, y) = \sqrt{\frac{x+y}{x-y}}$.

(c) $f(x, y) = \sqrt{1 - x^2y^2}$.

2. The function f is defined by $f(x, y) = \sqrt{x^2 + y^2}$.

- (a) In the xy -plane, sketch three level curves, at level 0, 1 and 4, and label each level curve appropriately.
- (b) Make a 3D-sketch of the surface $z = f(x, y)$.

Before making the sketch, determine what the intersection of the graph of f is with the coordinate planes, and sketch those first.

3. Write the following functions using polar coordinates r and θ , see *Thomas' Calculus*, page 647. Simplify as much as possible. In particular: retain only one power of r .

$$(a) f(x, y) = \frac{xy}{\sqrt{x^2 + y^2}}$$

$$(b) f(x, y) = \frac{x^2 - y^2}{x^2 + y^2}$$

$$(c) f(x, y) = \frac{x + 2y}{(x^2 + y^2)^{3/2}}$$

$$(d) f(x, y) = \frac{\sqrt{x^2 - xy + y^2}}{(x^2 + y^2)\sqrt{x^2 + y^2}}$$

4. Find $\frac{\partial f}{\partial x}$ and $\frac{\partial f}{\partial y}$ of the following functions:

(a) $f(x, y) = x^2 - xy + y^2$

(b) $f(x, y) = \cos^2(3x - y^2)$

5. Find second-order partial derivatives (g_{xx} , g_{xy} , g_{yx} , g_{yy}) of the function $g(x, y) = x^2y + \cos y + y \sin x$.

See *Thomas' Calculus*, page 788, for definitions and theorems.

6. (a) Find the equation for the tangent plane to the surface $z = \sqrt{x^2 + y^2 - 18}$ at the point $P(3, 5, 4)$.

(b) Find the linearization of $f(x, y) = \sqrt{x^2 + y^2 - 18}$ at $(3, 5)$, and use the linearization to approximate $f(2.9, 5.1)$.

See *Thomas' Calculus*, page 811, equation (4).